

scalable quantum-classical interfaces & applications to quantum learning



Univ.-Prof. Dr. Richard Kueng, MSc ETH
Department of **Quantum Information and Computation at Kepler (QUICK)**,
Johannes Kepler University Linz (AT)

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outline

- broad overview
- quantum readout problem
- classical shadows: new quantum-classical interfaces
- application: learning with quantum data
- synopsis

broad overview

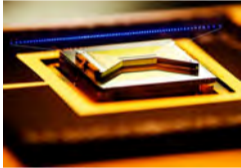


what is quantum computing?

- quantum computers are **not** next generation of supercomputers
- we try to **re-invent the wheel of computing** itself

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ions



neutral atoms



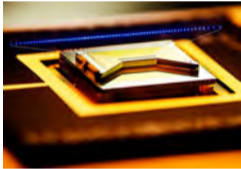
photons



superconducting circuits

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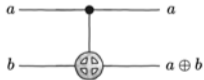
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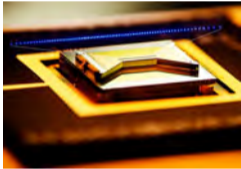


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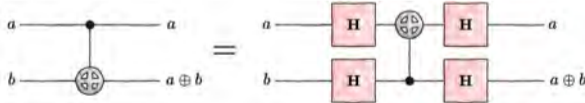
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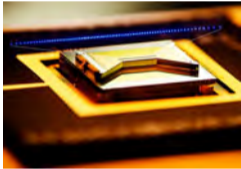


superconducting circuits

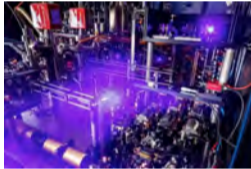


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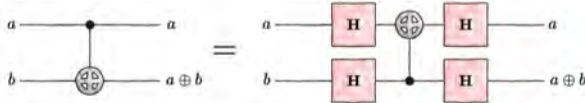
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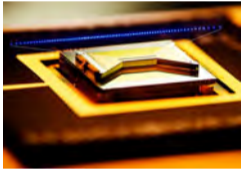


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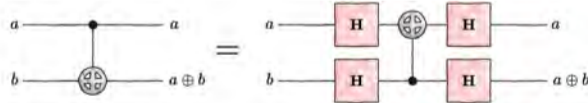
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superconducting circuits

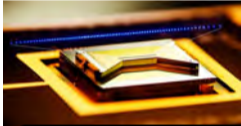


useful analogy:



what is quantum computing?

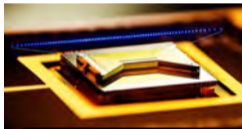
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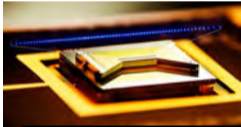
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- **memory** (quantum compression)
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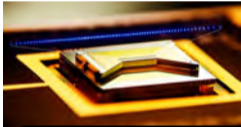
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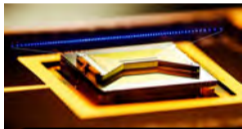
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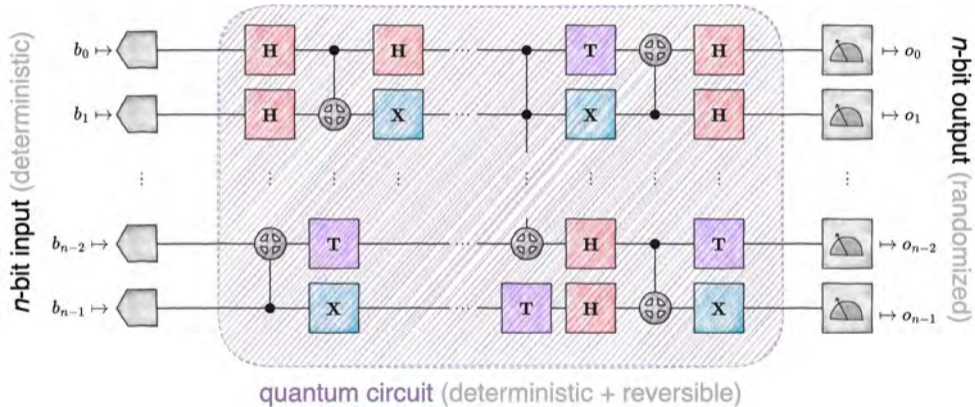


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identify tasks where quantum computers **justifiably** save **a lot of** resources:

- **runtime** (quantum speedup), e.g. Shor, HHL **too demanding near-term**
- **memory** (quantum compression) **requires unfavorable compromises**
- **training data size** (quantum-enhanced learning) **window of opportunity**

the quantum circuit model

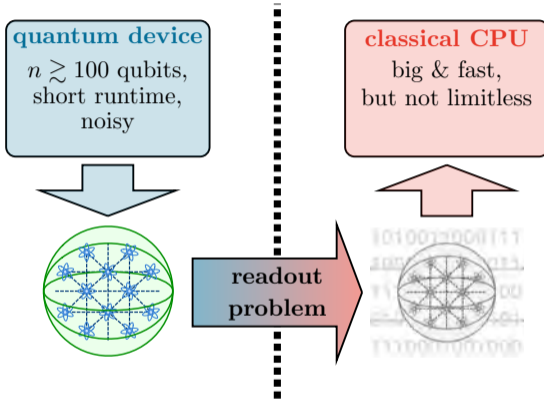


produces a **distribution** over all 2^n bit strings; result often encoded in **statistical correlations**

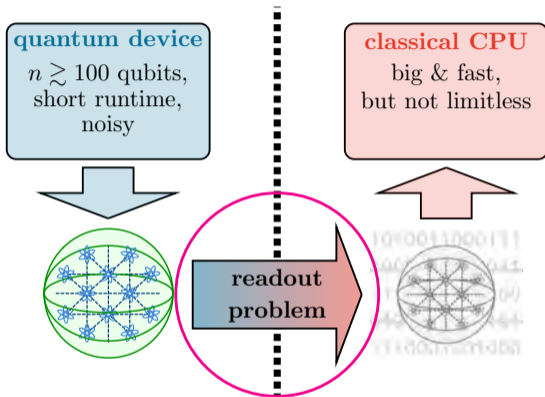
quantum readout problem



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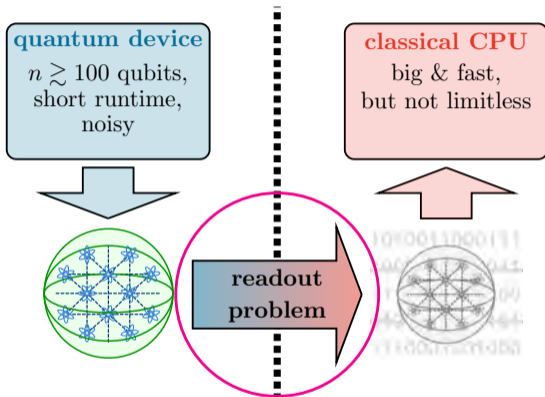


quantum readout problem



fundamental challenge
(often) exponential in qubit number

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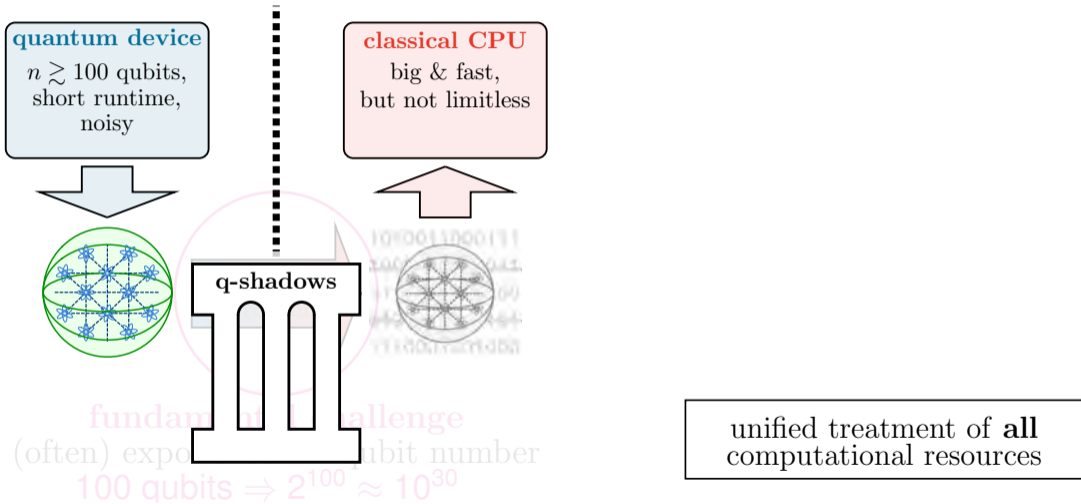


fundamental challenge

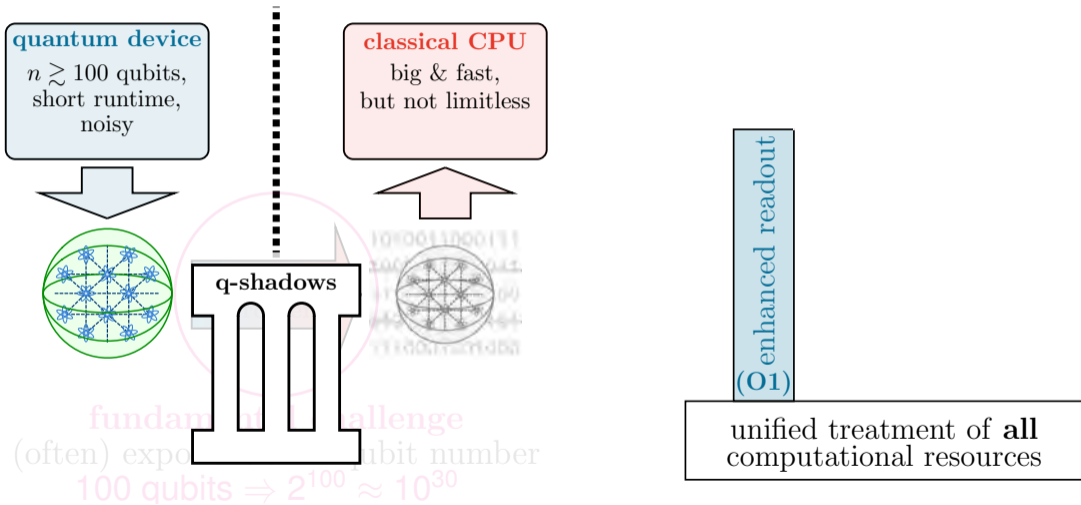
(often) exponential in qubit number

$$100 \text{ qubits} \Rightarrow 2^{100} \approx 10^{30}$$

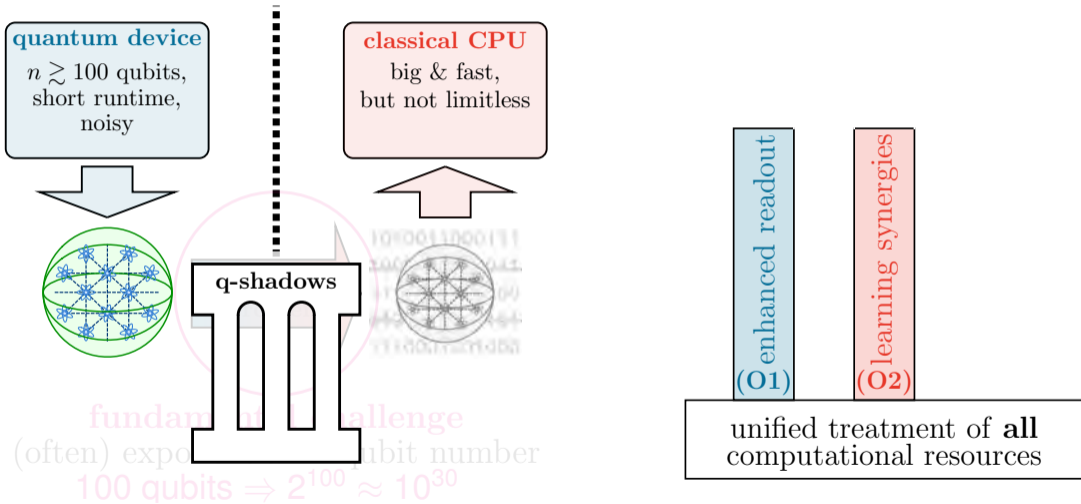
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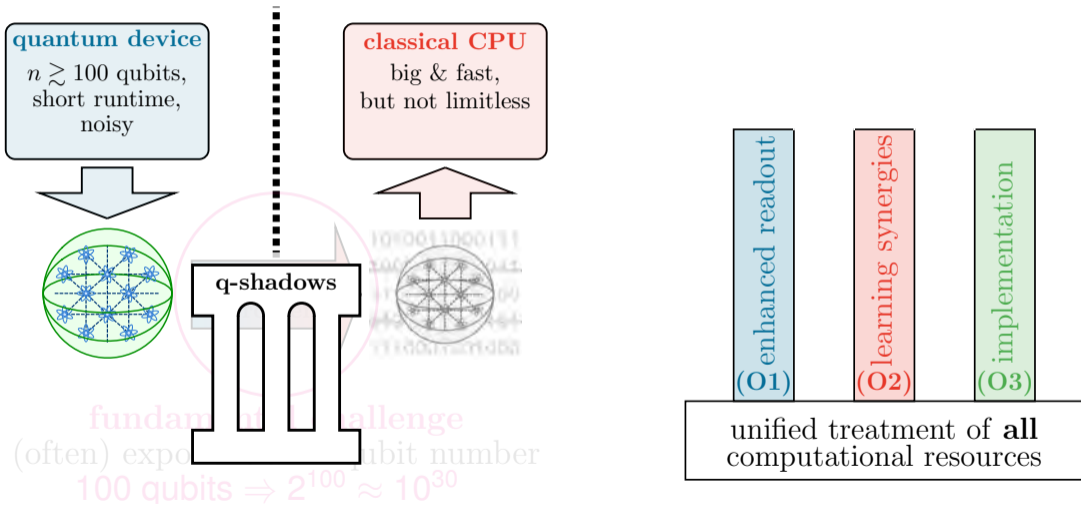
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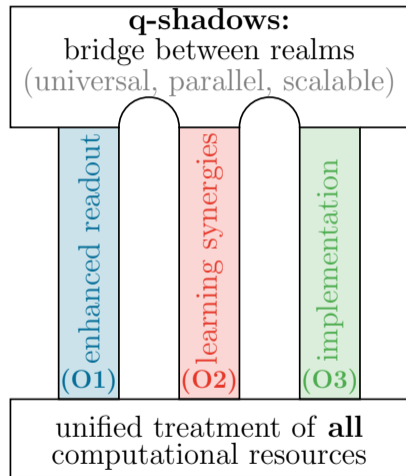
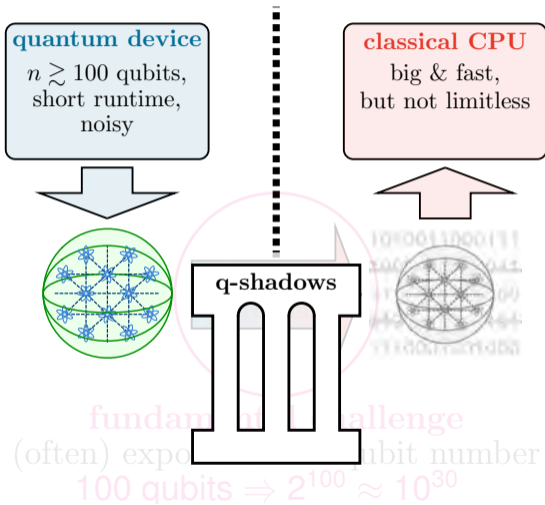
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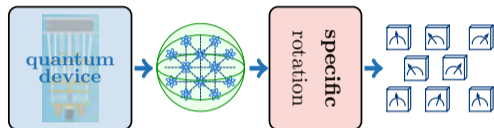


classical shadows: new quantum-classical interfaces



classical shadows: high-level overview

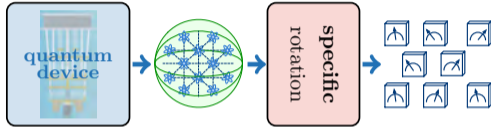
state of the art



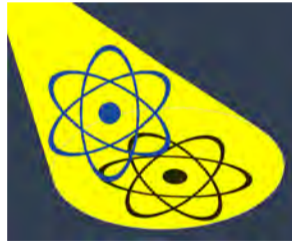
special purpose, sequential

classical shadows: high-level overview

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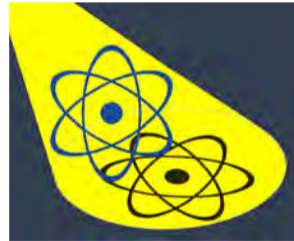
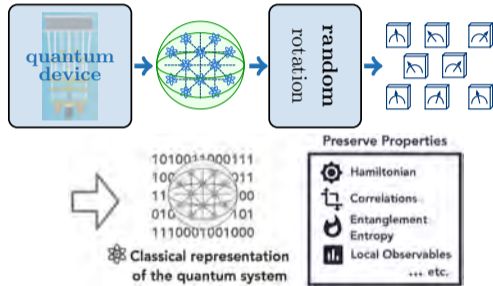


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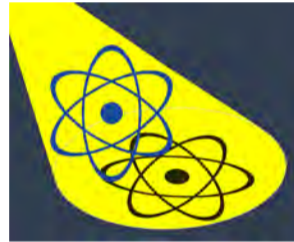
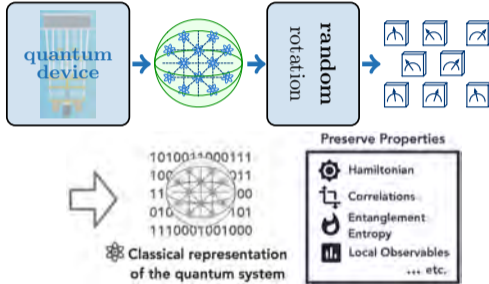
classical shadows: high-level overview

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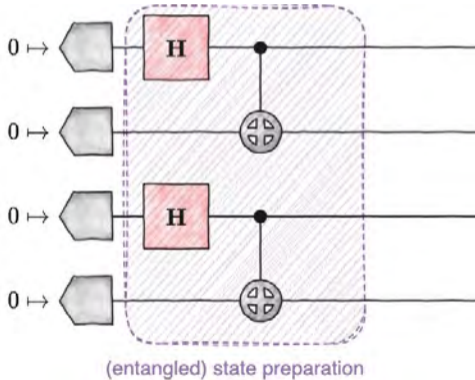
classical shadows



- classical shadows are new, universal & parallelizable (Huang, Kueng, Preskill, **Nature Physics** 2020)
- 2024 Bell prize for John Preskill

4 qubit case study: extracting properties directly

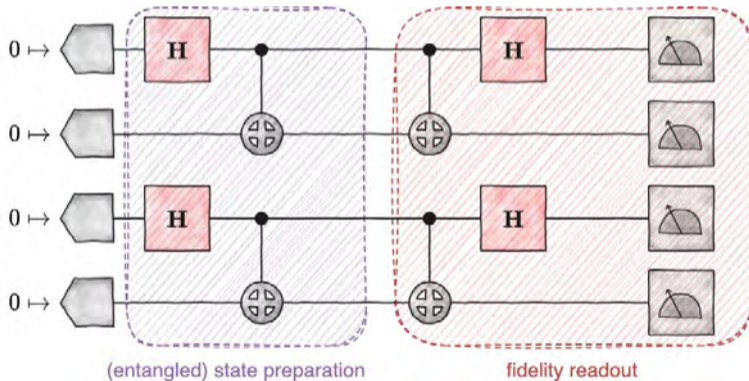
state preparation: two Bell states $\frac{1}{2} (|00\rangle + |11\rangle) \otimes (|00\rangle + |11\rangle)$



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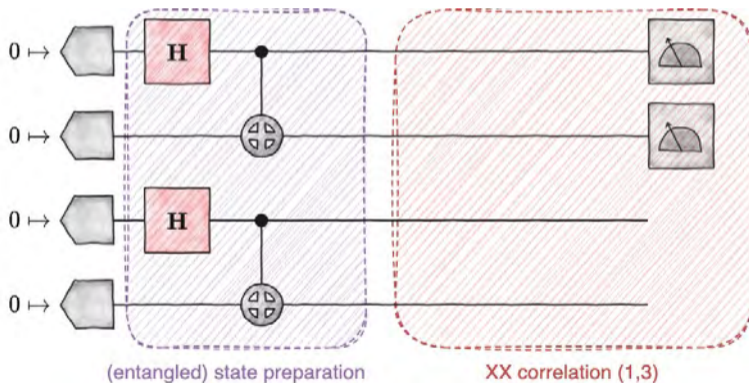
(T0) global fidelity with respect to target states



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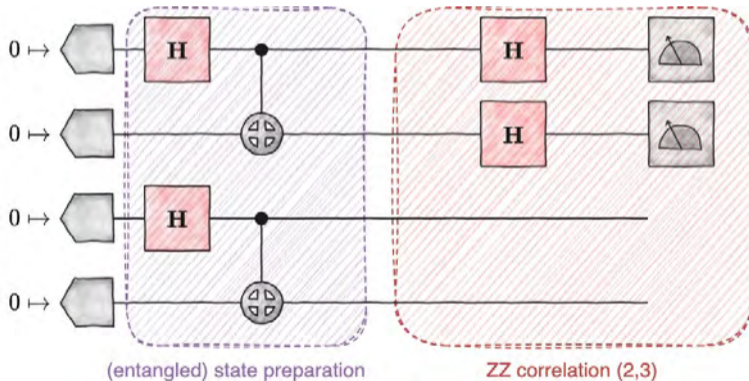
(T1a) ZZ correlations for qubits (0,1)



4 qubit case study: extracting properties directly

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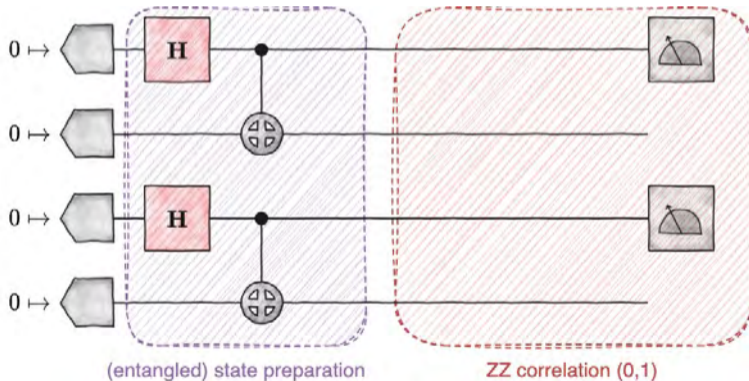
(T1b) XX correlations for qubits (0,1)



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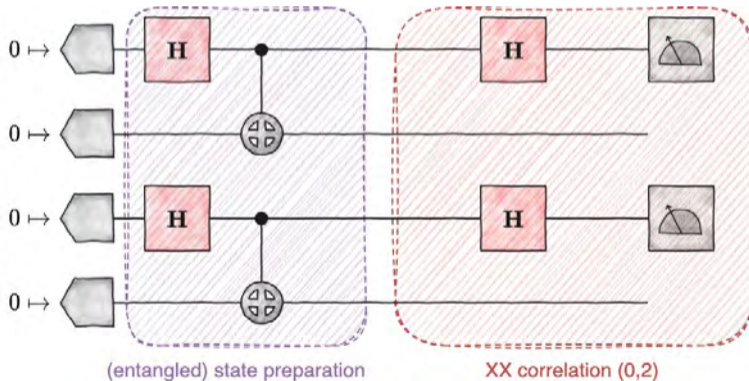
(T2a) ZZ correlations for qubits (0,2)



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state preparation: two Bell states $\frac{1}{2} (|00\rangle + |11\rangle) \otimes (|00\rangle + |11\rangle)$

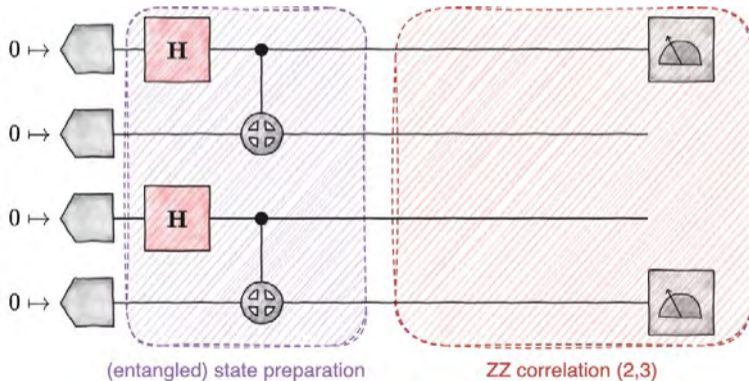
(T2b) XX correlations for qubits (0,2)



4 qubit case study: extracting properties directly

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(T3a) ZZ correlations for qubits (0,3)



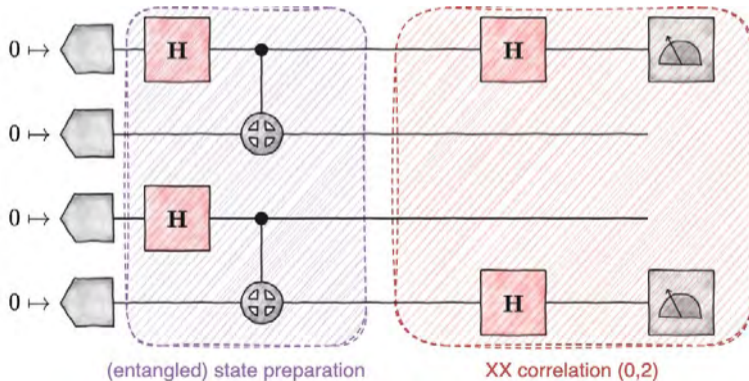
strategies to determine

- global fidelity
- two-bit correlations (Z)
- two-bit correlations (X)

4 qubit case study: extracting properties directly

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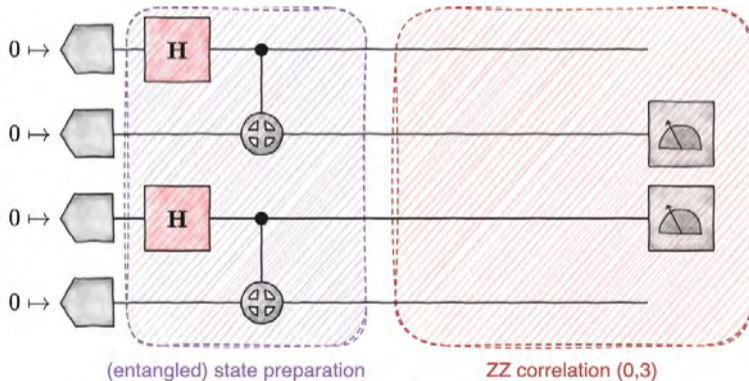
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4 qubit case study: extracting properties directly

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(T4a) ZZ correlations for qubits (1,2)



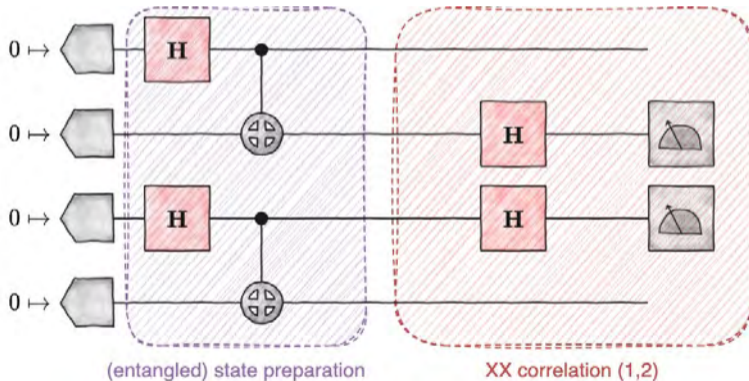
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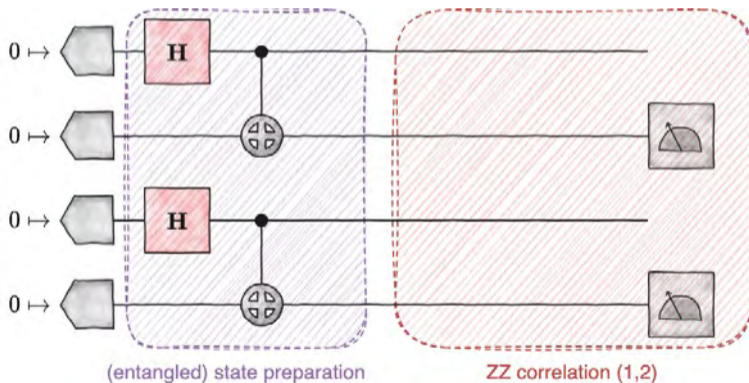
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(T5a) ZZ correlations for qubits (1,3)



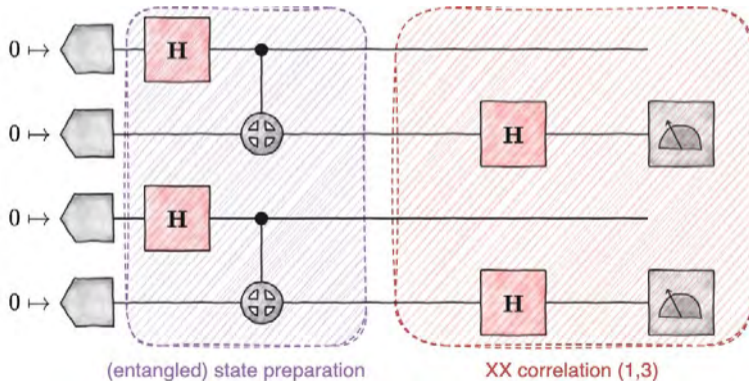
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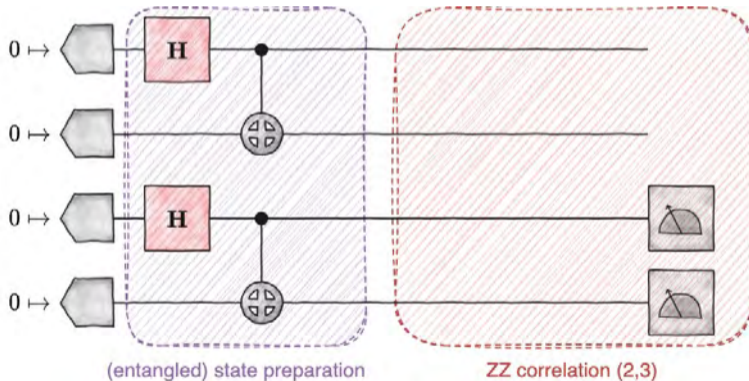
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state preparation: two Bell states $\frac{1}{2} (|00\rangle + |11\rangle) \otimes (|00\rangle + |11\rangle)$

(T6a) ZZ correlations for qubits (2,3)



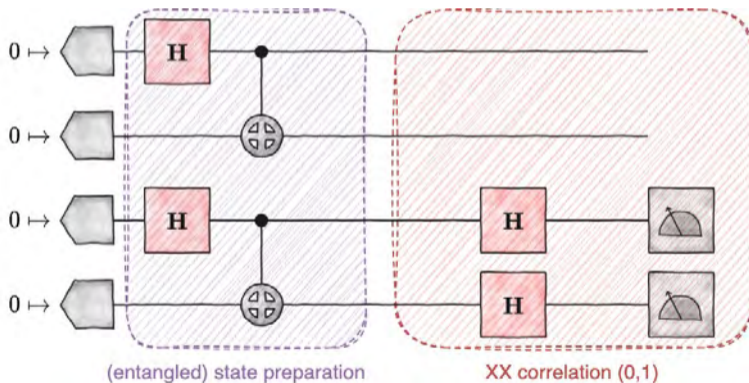
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(T6b) XX correlations for qubits (2,3)



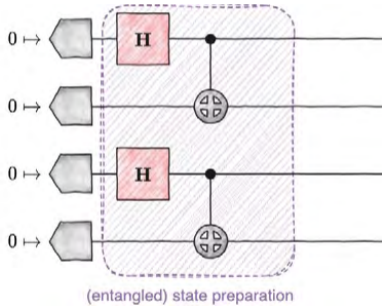
$$13 = 1 + 2 \times 6$$

strategies to determine

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- two-bit correlations (X)

4 qubit case study: classical shadows

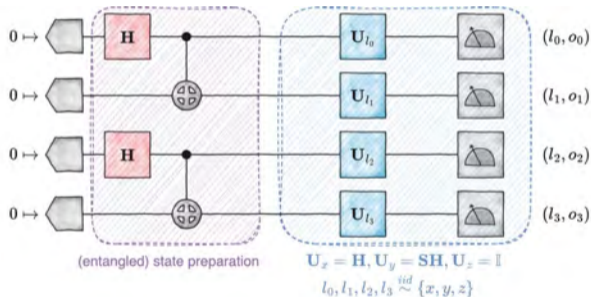
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4 qubit case study: classical shadows

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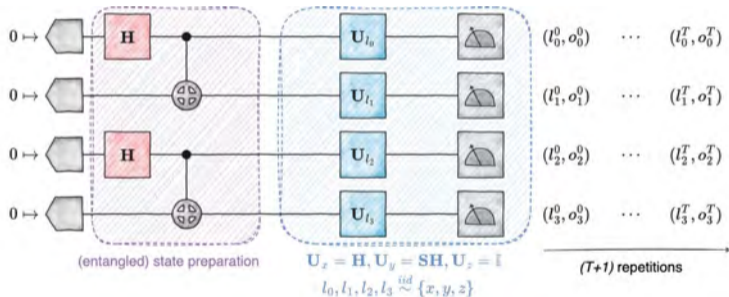
step 1: randomized readout (single-shot)



4 qubit case study: classical shadows

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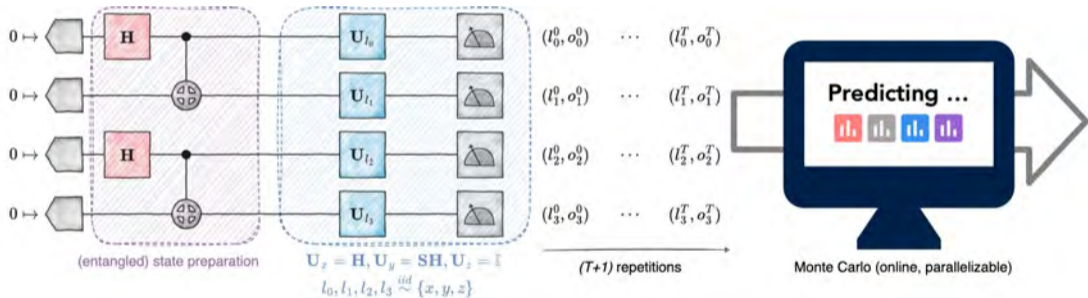
step 2: repeat T times with different random rotations



4 qubit case study: classical shadows

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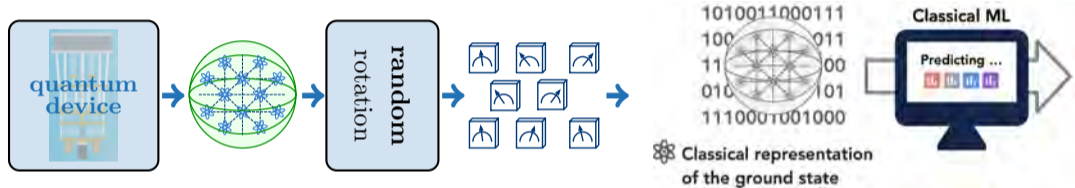
step 3: use classical data analysis to predict whatever you want **in parallel**



application: learning with quantum data



high-level vision



full quantum-classical learning pipeline:

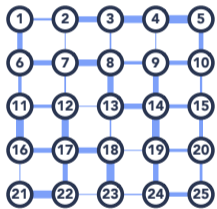
- o a quantum architecture prepares *interesting* quantum states
- o convert them into a classical shadow (new classical data format)
- o use these classical shadows as training data for a classical ML model

⇒ *classical machine learning with quantum data*

vignette application: many-body ground state properties

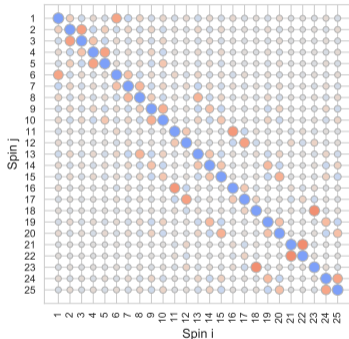
(a) 2D anti-ferromagnetic
random Heisenberg model

$$H = \sum_{\langle ij \rangle} J_{ij}(X_i X_j + Y_i Y_j + Z_i Z_j)$$

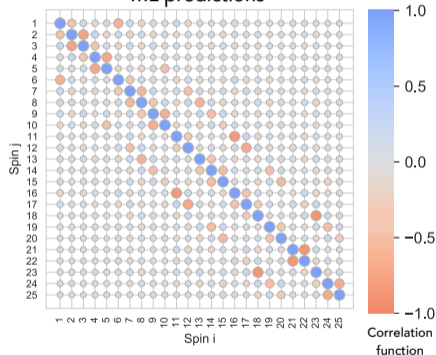


*The random J considered in (c)

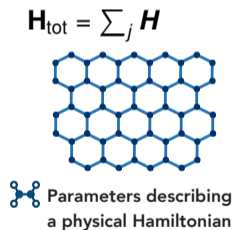
(b) Exact values from DMRG



ML predictions



vignette application: many-body ground state properties



direct computation

$$\rho(x) = \mathbf{v}_{\min}(x) \mathbf{v}_{\min}(x)^\dagger$$

(expensive: $D = 2^n$)



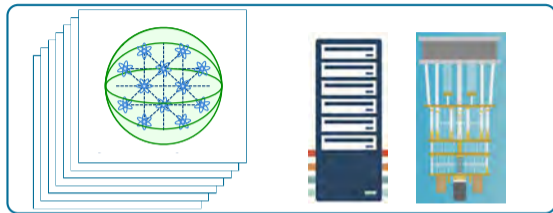
$\text{tr}(\mathbf{O}\rho(x))$

1010011000111
100000011
11000000
010000101
1110001001000



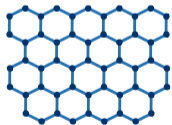
Classical representation of the ground state


vignette application: many-body ground state properties

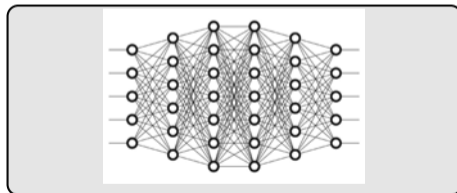


$$x \in [-1, 1]^m$$

$$\mathbf{H}_{\text{tot}}(X) = \sum_j \mathbf{H}(x_j)$$



 Parameters describing a physical Hamiltonian



$$(x_\ell, \rho(x_\ell)) \Downarrow x_\ell \sim \text{unif}[-1, 1]^m$$



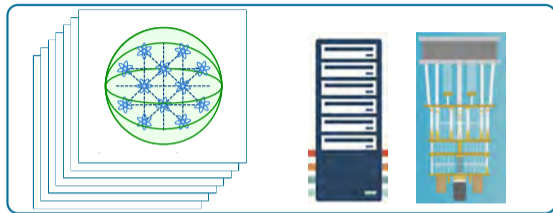
$$\text{tr}(\mathbf{O}\rho_{\text{train}}(x))$$

1010011000111
 100000011
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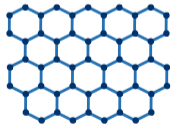
Classical representation of the ground state


vignette application: many-body ground state properties



$$x \in [-1, 1]^m$$

$$\mathbf{H}_{\text{tot}}(x) = \sum_j \mathbf{H}(x)$$



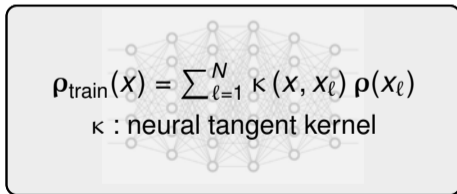
 Parameters describing a physical Hamiltonian



$$(x_\ell, \rho(x_\ell)) \Downarrow x_\ell \sim [-1, 1]^m$$

$$\rho_{\text{train}}(x) = \sum_{\ell=1}^N \kappa(x, x_\ell) \rho(x_\ell)$$

κ : neural tangent kernel



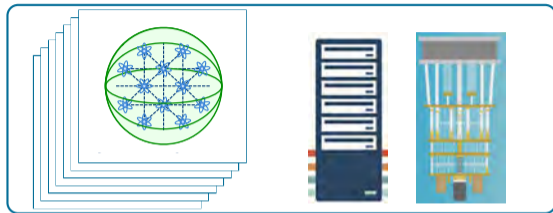
$$\text{tr}(\mathbf{O} \rho_{\text{train}}(x))$$

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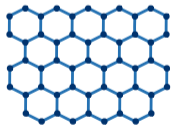
Classical representation of the ground state


vignette application: many-body ground state properties



$$x \in [-1, 1]^m$$

$$\mathbf{H}_{\text{tot}}(X) = \sum_j \mathbf{H}(x_j)$$



 Parameters describing a physical Hamiltonian




$$(x_\ell, \rho(x_\ell)) \Downarrow x_\ell \sim [-1, 1]^m$$

$$\rho_{\text{train}}(X) = \sum_{\ell=1}^N \kappa(X, x_\ell) \rho(x_\ell)$$

κ : neural tangent kernel
 κ : ℓ_2 -Dirichlet kernel



$$\text{tr}(\mathbf{O} \rho_{\text{train}}(X))$$


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Classical representation of the ground state

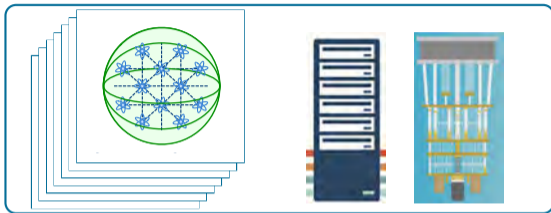
vignette application: many-body ground state properties

Theorem: assumptions on $\mathbf{H}(x)$, \mathbf{O} ensure

$$\mathbb{E}_{x \sim [-1,1]^m}^{unif} |\text{tr}(\mathbf{O}\rho_{\text{train}}(x)) - \text{tr}(\mathbf{O}\rho(x))|^2 \leq \epsilon$$

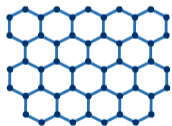
(MSE $\leq \epsilon$) with $\text{poly}(m) = \text{poly}(n)$ scaling in


- training data size
- runtime + memory



$$x \in [-1, 1]^m$$

$$\mathbf{H}_{\text{tot}}(x) = \sum_j \mathbf{H}(x)$$



 Parameters describing a physical Hamiltonian



$$\rho_{\text{train}}(x) = \sum_{\ell=1}^N \kappa(x, x_{\ell}) \rho(x_{\ell})$$

κ : neural tangent kernel

κ : ℓ_2 -Dirichlet kernel

$$(x_{\ell}, \rho(x_{\ell})) \Downarrow x_{\ell} \sim [-1, 1]^m$$



$$\text{tr}(\mathbf{O}\rho_{\text{train}}(x))$$

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11000000
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Classical representation of the ground state

main result

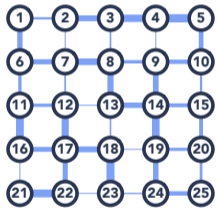
Theorem 1 (Learning to predict ground state representations; informal). *For any smooth family of Hamiltonians $\{H(x) : x \in [-1, 1]^m\}$ in a finite spatial dimension with a constant spectral gap, the classical machine learning algorithm can learn to predict a classical representation of the ground state $\rho(x)$ of $H(x)$ that approximates few-body reduced density matrices up to a constant error ϵ when averaged over x . The required training data size N and computation time are polynomial in m and linear in the system size n .*

- H.Y. Huang, R. Kueng, G. Torlai, V.A. Albert, J. Preskill. *Provably efficient ML for many-body problems.* **Science** **377**, eabk3333 (2022)
- L. Lewis, H.Y. Huang, V.T. Tran, S. Lehner, R. Kueng, J. Preskill. *Improved machine learning algorithm for predicting ground state properties.* **Nature Communications** **15**, 895 (2024)

numerics: 2D Heisenberg model with $n = 25$ spins

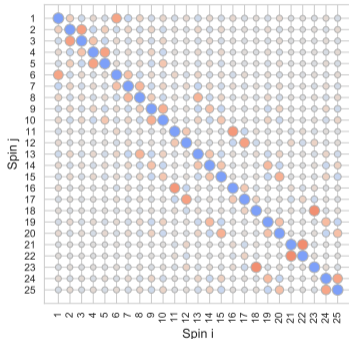
(a) 2D anti-ferromagnetic
random Heisenberg model

$$H = \sum_{\langle ij \rangle} J_{ij}(X_i X_j + Y_i Y_j + Z_i Z_j)$$

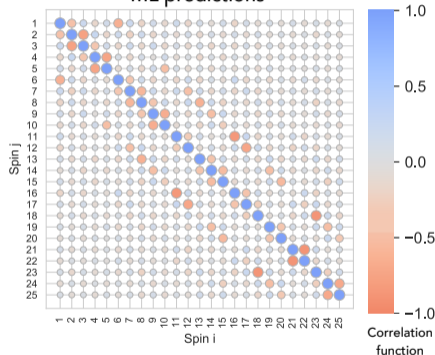


*The random J considered in (c)

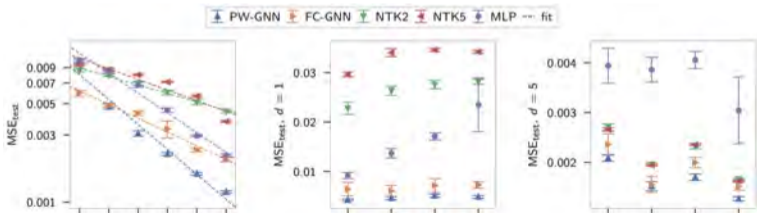
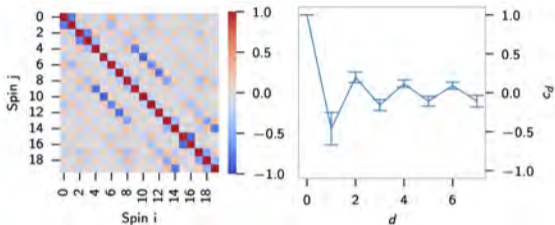
(b) Exact values from DMRG



ML predictions



numerics: 2D Heisenberg model with different ML models



comparison between


- NKT (green, red)
- MLP (purple)
- GNN (blue, orange)

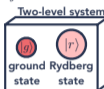
collaboration with Caltech
and Hochreiter group (JKU)

[Tran *et al*, NeurIPS workshop 22]

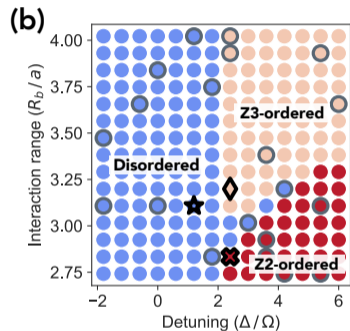
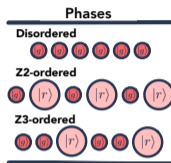
numerics: 1D chain of $n = 51$ Rydberg atoms



(a)
$$H = \sum_i \frac{\Omega}{2} X_i - \sum_i \Delta N_i + \sum_{i < j} \Omega \left(\frac{R_b}{a|i-j|} \right)^6 N_i N_j$$




Rydberg atom array  a : atom separation

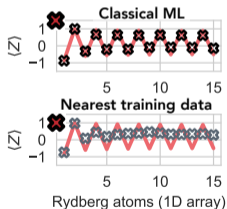
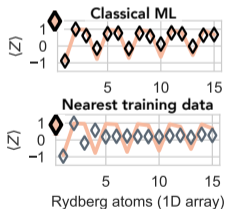
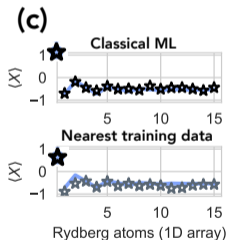
Two-level system 

$$N_i = |r_i\rangle\langle r_i|, \quad X_i = |g_i\rangle\langle r_i| + |r_i\rangle\langle g_i|, \quad Z_i = |g_i\rangle\langle g_i| - |r_i\rangle\langle r_i|$$



 ...  : Training data (a total of 20)

   : Testing point (predict ground state)

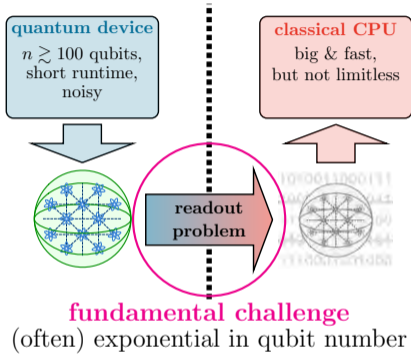


*Solid lines in the six line plots indicate exact values from DMRG

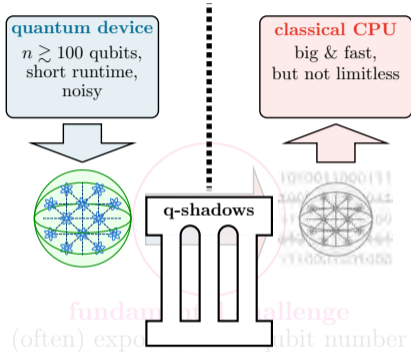
synopsis



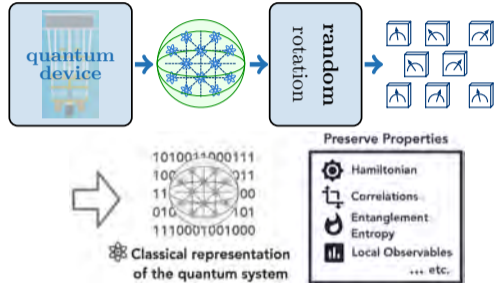
synopsis



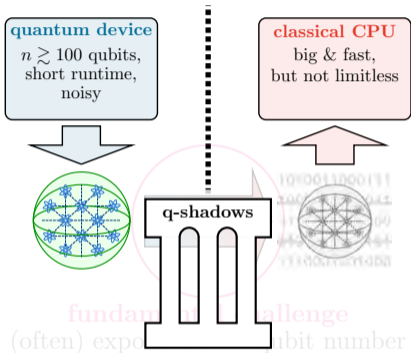
synopsis



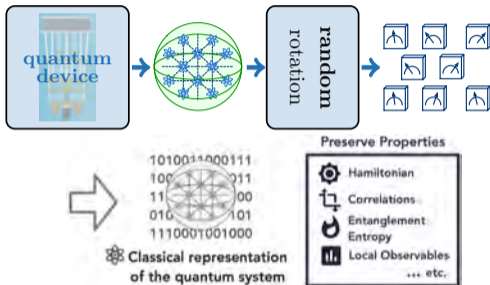
classical shadows (quantum-classical interfaces)



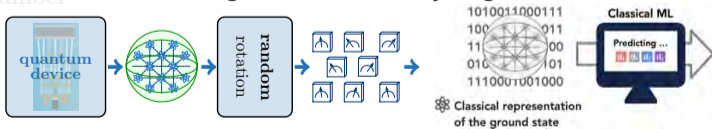
synopsis



classical shadows (quantum-classical interfaces)




rigorous+efficient synergies with ML




QUICK department at Johannes Kepler University Linz

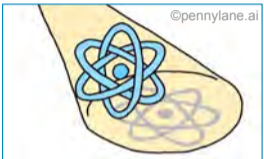
Quantum Information & Computation at Kepler



Johannes Kofler
 → quantum information
 → quantum foundations

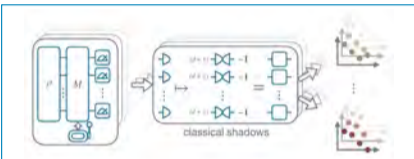


Richard Kueng (chair)
 → quantum computing
 → (convex) optimization
 → math of data science



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Classical shadow formalism











Hybrid quantum-classical algorithms

"Don't mind your make-up, you'd better make your mind up." Frank Zappa

Join our team:
 → PhD student
 → Postdoc



Team

							
Nina Brandl	Michaela Eder-Jahn	Sebastian Egginger	Kristina Kirova	Elisabeth Peheim	Alexander Ploier	Viet Tran	Jadwiga Wilkens



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